

Hydrogels in drug delivery

Control of drug release kinetics by hydrogel structure^{6,7}

- Release from stable hydrogels is controlled by diffusion of solute through the network
- Diffusion is described by Fick's second law:

$$\text{Eqn 1} \quad \frac{\partial C}{\partial t} = D_{gel} \frac{\partial^2 C}{\partial x^2}$$

- Recall the solution to Fick's second law for a semi-infinite slab contacting a perfect sink:

$$\text{Eqn 2} \quad \frac{c_0 - c(x)}{c_0} = 1 - \text{erf}\left(\frac{x}{2\sqrt{tD}}\right)$$

- Diffusion of drugs through a network is controlled by the mesh size (ζ)

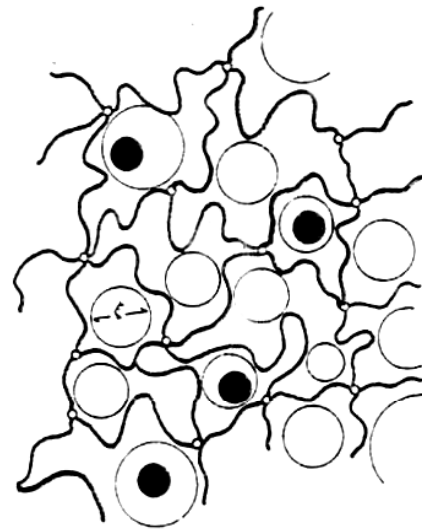
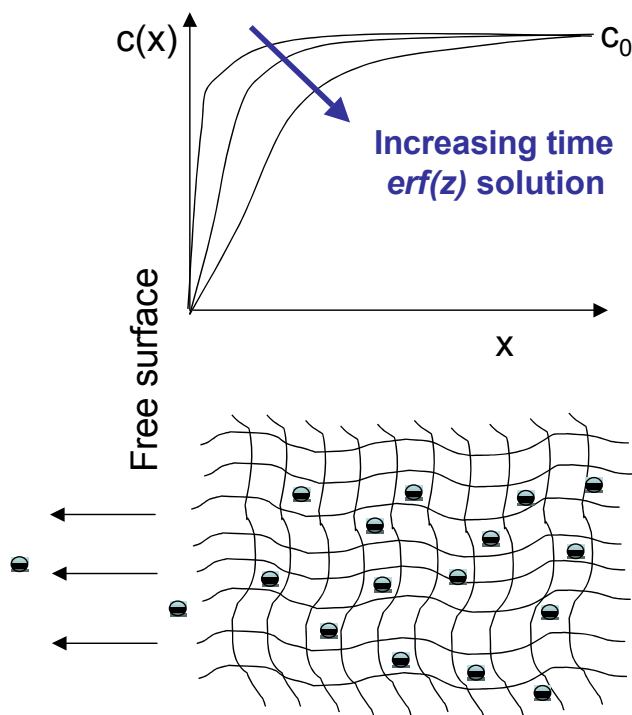
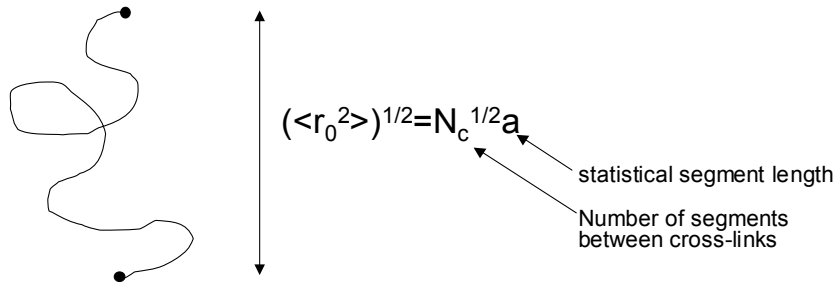


Fig. 3. Crosslinked structure of a polymer gel, showing effective chains of the structure defined by crosslinks. The effective area for diffusion for the solute is characterized by an average mesh size ζ . The smaller solutes, illustrated as dark circles, must pass between the macromolecules.

- The mesh size is related to the network swelling Q and the end-to-end distance between cross-links:



Eqn 3
$$(\bar{r}_0^2)^{1/2} = \left(\frac{2M_c}{M_0} \right)^{1/2} C_n^{1/2} l$$

- ...assuming a polymer chain that has 2 carbon-carbon bonds per repeat unit
- derived from random walk chain statistics
 - Where l is the bond length in the polymer backbone
 - M_c is the molecular weight between cross-links
 - M_0 is the molecular weight per repeat unit
 - Where C_n is the characteristic ratio for the polymer chain

Eqn 4
$$\xi = \frac{(\bar{r}_0^2)^{1/2}}{\phi_{2,s}^{1/3}} = Q^{1/3} (\bar{r}_0^2)^{1/2} = C_n^{1/2} Q^{1/3} N^{1/2} l$$

- Q is the degree of swelling = $V_{\text{swollen polymer}} / V_{\text{dry polymer}}$
- N is the degree of polymerization between cross-links
- The mesh size is related to the diffusion constant of a solute in the network
- Eyring theory of diffusion:

Eqn 5
$$D = T v e^{-\frac{\Delta G^*}{kT}} = T v e^{-\frac{\Delta H^*}{kT}} e^{\frac{\Delta S^*}{k}}$$

- Where ΔG^* is the activation energy, ΔH^* is activation enthalpy, and ΔS^* is activation entropy
- N = translational oscillating frequency of solute molecule (jump rate!)
- T = temperature
- k = Boltzman constant
- The ratio of diffusion constant in the gel to that in solution is:

Eqn 6
$$\hat{D} = \frac{D_{gel}}{D_0} = \frac{e^{\frac{\Delta S_{gel}^*}{k}}}{e^{\frac{\Delta S_0^*}{k}}}$$

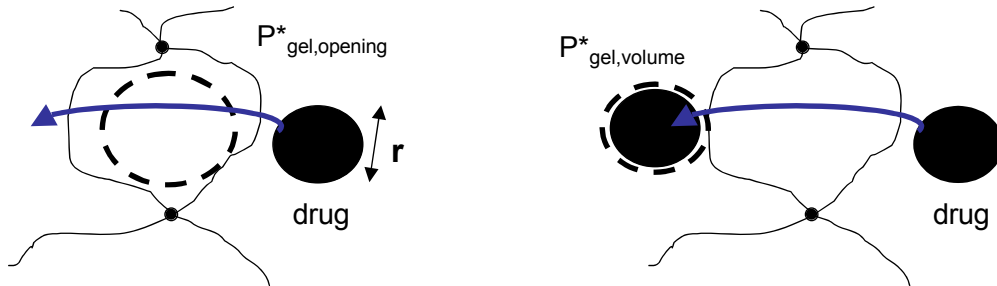
- Where ΔS_{gel}^* is the activation entropy for diffusion in the gel and ΔS_0^* is the activation entropy in for diffusion in the solvent
- This assumes the activation enthalpy and oscillation frequencies for diffusion are approximately the same in the gel and pure solvent (reasonable for dilute and chemically inert systems)
- The activation entropies are:

Eqn 7
$$\Delta S_{gel}^* = k \ln P^* - k \ln P_0$$

Eqn 8 $\Delta S^*_0 = k \ln P^*_0 - k \ln P_0$

Eqn 9 $\hat{D} = \frac{P^*_{gel}}{P^*_0} = \frac{P^*_{gel,opening} P^*_{gel,volume}}{P^*_{0,volume}}$

- Where P*volume is the probability that a solute-sized volume of free space exists to jump into
- P*opening is the probability that the network has a solute-sized gap to jump through



Eqn 10 $P^*_{gel,opening} = \frac{\xi - r}{\xi} = 1 - \frac{r}{\xi}$

- Where r is the size of the solute (drug) and xi is the network mesh size
- The probability of a volume to jump into is an exponential of the ratio of the solute size to the available free volume per mole:

Eqn 11 $P^*_{gel,volume} \sim e^{-\frac{v^*}{v_{free,gel}}}$

Eqn 12 $P^*_{0,volume} \sim e^{-\frac{v^*}{v_{free,1}}}$

- Where vfree is the specific free volume and v* is the volume of the solute (drug)
- Refs for free volume theory applied here:
 - Yasuda et al. Makromol. Chem. 26, 177 (1969)
 - Peppas and Reinhart, J. Membrane Sci. 15, 275 (1983)
- Now:

Eqn 13 $\frac{P^*_{gel,volume}}{P^*_{0,volume}} = e^{-\left(\frac{v^*}{v_{free,gel}} - \frac{v^*}{v_{free,1}}\right)}$

- The free volume in a swollen gel is approximately vfree,1 since the free volume contribution from polymer is extremely low (2.5% even in solid polymers at 25°C)

Eqn 14 $v_{free,gel} = \phi_1 v_{free,1} + \phi_2 v_{free,2}$

- Therefore:

Eqn 15 $v_{free,gel} \sim \phi_1 v_{free,1} = (1 - \phi_2) v_{free,1} = (1 - 1/Q) v_{free,1}$

- Where Q is the swelling degree = $V_{swollen\ gel} / V_{dry\ gel} = 1/\phi_2$
- Therefore:

$$\text{Eqn 16} \quad \frac{P_{gel,volume}^*}{P_{0,volume}^*} = e^{-\left(\frac{v^*}{(1-\frac{1}{Q})v_{free,1}} - \frac{v^*}{v_{free,1}}\right)} = e^{-\frac{v^*}{v_{free,1}}\left(\frac{1}{Q-1}\right)} \approx e^{-\left(\frac{1}{Q-1}\right)}$$

○ $v^*/v_{free,1} \sim 1$ for most polymers, experimentally

- Therefore:

$$\text{Eqn 17} \quad \hat{D} \cong \left(1 - \frac{r}{\xi}\right) e^{\left[\frac{-1}{(Q-1)}\right]}$$

- And thus finally:

$$\text{Eqn 18} \quad D_{gel} \cong D_0 \left(1 - \frac{r}{\xi}\right) e^{\left[\frac{-1}{(Q-1)}\right]}$$

○ Insulin: MW – 5900 g/mole; hydrodynamic radius = 16 Å

References

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